



A6.5 Backus-Naur Form and syntax diagrams

Theory of computation · A level · AQA 7517 4.4.3.1, Eduqas A500QS 1.8 ·
about 25 min

Name _____

Class _____

Date _____

What this lesson is about

Production rules, syntax diagrams, a grammar for robot programs, recursive descent, and why BNF can describe what a regex cannot.

- Production rules
- A robot command language
- Syntax diagrams
- Why BNF can do what a regex cannot
- Checking syntax with recursion

Questions

6 marks in all

- In BNF, what does ::= mean? [1 mark]
 - ☐ A Is equal to
 - ☐ B Is defined as
 - ☐ C Or
 - ☐ D Is followed by
- Using $\langle \text{integer} \rangle ::= \langle \text{digit} \rangle \mid \langle \text{digit} \rangle \langle \text{integer} \rangle$ and $\langle \text{move} \rangle ::= \langle \text{direction} \rangle \langle \text{integer} \rangle$ with $\langle \text{direction} \rangle ::= \text{F} \mid \text{B} \mid \text{L} \mid \text{R}$, which are valid moves? [1 mark]

Tick every answer that is true.

 - ☐ A F20
 - ☐ B R7
 - ☐ C F
 - ☐ D 20F
 - ☐ E L005
- Why can BNF describe some languages that regular expressions cannot? [1 mark]
 - ☐ A BNF allows alternatives with |
 - ☐ B BNF rules can be recursive in the middle of a rule, so they can describe nesting such as balanced brackets
 - ☐ C BNF uses angle brackets
 - ☐ D BNF can only describe finite languages
- In a syntax diagram, what does a path that loops back round a box show? [1 mark]
 - ☐ A The item may be skipped
 - ☐ B The item may be repeated
 - ☐ C The item is a terminal
 - ☐ D The syntax is invalid

5. Given $\langle s \rangle ::= ab \mid a\langle s \rangle b$, how many times must the rule be used to produce aaabbb?

[1 mark]

6. What does this program print?

[1 mark]

```
def s(text, i):
    if text[i:i + 2] == "ab":
        return i + 2
    if text[i:i + 1] == "a":
        j = s(text, i + 1)
        if j != -1 and text[j:j + 1] == "b":
            return j + 1
    return -1

for t in ["aabb", "aab", "abb"]:
    print(t, s(t, 0))
```

The task: check robot programs

Write a recursive descent checker for the robot command language above and use it on the strings in `tests`.

- Write one function per rule you need, each taking `(text, i)` and returning the position after the match, or -1 if it does not match. At least `program`, `command` and `integer`.
- A string is valid only if `program` matches all of it.
- Check the nesting with your functions. Do not use the `re` module: no regex can check matched brackets.
- For each string in `tests`, in order, print the string, a space, then `valid` or `invalid`. For example `F20R90 valid`. Eight lines in all.

```
# the two lines every program starts with: the commands, then the robot
from bugbot import *
connect()

tests = ["F20R90", "[4F20R90]", "[2F10[3L5]]", "F20R", "[4F20", "4F20", "[3]", "F1"]

def integer(text, i):
    return -1
```

Plan your program here, then type it in and press Run.



Do it on the robot

www.bugbotlab.com/learn/a6-5-bnf-and-syntax-diagrams/

The simulator checks it and tells you when it passes. Nothing to install, no account.

Challenges

1. Add a rule so a program may contain `S`, meaning stop, as a command on its own. Change both the BNF and the syntax diagram.
2. Write BNF for a signed integer that may start with `+` or `-`.
3. Is the language of your `<integer>` rule regular? Write a regex for it. Is `<program>` regular?