



What this lesson is about

The edge between what is known and what is not, and why a map with holes is still useful.

- The definition
- From cells to targets
- Watching exploration saturate
- Shadows
- When it goes wrong

Questions

6 marks in all

1. What does this program print?

[1 mark]

```
rows = ["FFU",
        "FOFU",
        "FFFF",
        "UUFF"]
H, W = len(rows), len(rows[0])
count = 0
for r in range(H):
    for c in range(W):
        if rows[r][c] == "F":
            for dr, dc in ((1, 0), (-1, 0), (0, 1), (0, -1)):
                rr, cc = r + dr, c + dc
                if 0 <= rr < H and 0 <= cc < W and rows[rr][cc] == "U":
                    count += 1
                    break
print(count)
```

Answer:

6

F is free, O occupied, U unknown. The free cells with an unknown cell above, below, left or right are (0,2), (1,2), (2,0), (2,1), (2,3) and (3,2), so 6 frontier cells. (2,2) is free but all four of its neighbours are known.

2. Why is driving to a frontier cell guaranteed to produce new information?

[1 mark]

- ☐ A It is free, so it can be reached, and it borders a cell no beam has ever reached
- ☐ B It is always the cell furthest from the robot
- ☐ C It is next to an occupied cell, so the robot will see a wall
- ☐ D Its log odds are exactly zero

Answer: A. A frontier is a free cell with at least one unknown neighbour. When none are left and everywhere is reachable, the map is finished and the robot knows it.

3. Why can a feature map not support frontier exploration? [1 mark]

- ☐ A Absence from its list means both "not there" and "never looked", so it cannot say "unknown"
- ☐ B Feature maps cannot store positions accurately enough
- ☐ C Feature maps use too much memory for large rooms
- ☐ D Feature maps have no free cells to drive to

Answer: A. The grid distinguishes free, occupied and unknown, and the third kind is the one exploration needs.

4. Put the frontier exploration pipeline in order. [1 mark]

Number the lines 1 to 5 to put them in the right order.

- ___ Group adjacent frontier cells into regions with a flood fill
- ___ Discard regions smaller than the robot
- ___ Score each remaining region
- ___ Find every free cell with an unknown neighbour
- ___ Drive to the best one

Answer:

Find every free cell with an unknown neighbour
Group adjacent frontier cells into regions with a flood fill
Discard regions smaller than the robot
Score each remaining region
Drive to the best one

Individual frontier cells come in thousands, so they are grouped, the noise is thrown away, and only then is a target chosen.

5. The robot alternates for ever between two frontiers of equal value on opposite sides of the room. What is the fix? [1 mark]

- ☐ A Hysteresis: keep the current target until it is reached or disappears
- ☐ B Discard frontier regions smaller than the robot
- ☐ C Use eight neighbours instead of four
- ☐ D Lower L_MAX so the map changes its mind faster

Answer: A. This is ping-pong. Discarding small regions fixes a different failure, the sliver of unknown along a wall that never closes.

6. A small post leaves a wedge of unknown behind it. Why does moving a short distance sideways often beat driving a long way forward? [1 mark]

- ☐ A A second viewpoint a little apart sees round the post and resolves nearly all of the shadow
- ☐ B Sideways motion gives less odometry error
- ☐ C The sensor has a longer range sideways
- ☐ D Driving forward would make the robot collide with the post

Answer: A. The shadow widens with distance from a single viewpoint, so a small change of viewpoint uncovers a large area.

The task: what have I not seen?

Turn on the spot, building a grid as you go. Plot `known`, then print `explored:`, the fraction of cells that are no longer unknown, and `frontier:`, how many free cells have an unknown neighbour.

```
from bugbot import *
import math
connect()

CELL, W = 5.0, 40
L_OCC, L_FREE, L_MAX, FAR = 0.85, -0.4, 8.0, 170.0
START_X, START_Y = 100.0, 100.0
grid = [0.0] * (W * W)
```

The hint students can ask for: Turn on the spot for a good while, integrating every scan into the grid. A cell is unknown while its log odds is near zero; a frontier cell is a free one with an unknown neighbour. Count both, and plot the known fraction so you can watch it stop rising.

A solution

```
from bugbot import *
import math
connect()

CELL, W = 5.0, 40
L_OCC, L_FREE, L_MAX = 0.85, -0.4, 8.0
FAR = 170.0
START_X, START_Y = 100.0, 100.0
grid = [0.0] * (W * W)

def bump(x, y, amount):
    c, r = int(x / CELL), int(y / CELL)
    if 0 <= c < W and 0 <= r < W:
        i = r * W + c
        grid[i] = max(-L_MAX, min(L_MAX, grid[i] + amount))

def integrate():
    px, py = position()
    x, y = START_X + px, START_Y + py
    h = heading()
    for a, d in scan():
        th = math.radians(h + a)
        sx, sy = math.sin(th), math.cos(th)
        r = 0.0
        while r < min(d, FAR) - CELL:
            bump(x + r * sx, y + r * sy, L_FREE)
            r += CELL / 2
        if d < FAR:
            bump(x + d * sx, y + d * sy, L_OCC)

def explored():
    return sum(1 for v in grid if abs(v) > 1.0) / float(W * W)

drive(0, 0, 30)
for tick in range(150):
    integrate()
    plot("known", explored())
```

```

    wait(0.1)
    stop()
    integrate()

    print("explored:", round(explored(), 3))

    # a frontier cell is a free cell with an unknown neighbour: the edge of what is known
    frontier = 0
    for r in range(W):
        for c in range(W):
            if grid[r * W + c] >= -1.0:
                continue
            for dc, dr in ((1, 0), (-1, 0), (0, 1), (0, -1)):
                c2, r2 = c + dc, r + dr
                if 0 <= c2 < W and 0 <= r2 < W and abs(grid[r2 * W + c2]) <= 1.0:
                    frontier += 1
                    break
    print("frontier:", frontier)

```

Any program that meets the task's checks is marked correct in the simulator; this is one way, not the only way.